Number of solutions to a system of linear equations

Prove that it is impossible for a system of linear equations to have more than 1 but finitely many solutions. Hint: suppose (x_1, \ldots, x_n) and (y_1, \ldots, y_n) are distinct solutions. Show that there are then infinitely many solutions.