

### **A function continuous only on the irrationals**

(Very hard) Does there exist a function  $f : \mathbb{R} \rightarrow \mathbb{R}$  (i.e., the domain is the real numbers and every value is a real number) such that  $f(x)$  is only continuous at irrational numbers?