## Number Bases - examples

- (1) Convert  $73_8$  to base 10.
- (2) Convert 162 to base 5.
- (3) Convert  $101101011_2$  to base 10.
- (4) Convert 617 to base 2.
- (5) Convert  $113_6$  to base 9.
- (6) If 4 + 5 = 10 in some base b, what is b?
- (7) If  $6 \times 4 = 33$  in some base b, what is b?
- (8) If 15 + 21 = 40 in some base *b*, what is *b*?
- (9) If  $4 \times 6 = 30$  in some base, then what is 5! in this base?
- (10) A base-two numeral consists of 15 digits all of which are ones. This number when tripled and written in base two, contains how many digits?
- (11) Show that  $10 \times 10 = 100$  in any base b.
- (12) Suppose that  $37_b$  is exactly half of  $73_b$ . What is b?
- (13) Suppose that a certain integer x can be written as a two-digit number in both bases 5 and 6 where the first digit is 4. That is,  $x = \underline{4y}_5$  and  $x = \underline{4z}_6$  for some digits y, z. What is x (in base 10)?
- (14) A positive integer n can be written in base 7 as the three-digit number xyy. The same number n can be written in base 6 as the three-digit number yxx. Find n.
- (15) Let x and y be digits in base 7 such that

$$1111_2 + 1111_3 + 1111_4 + 1111_5 + 1111_6 + 1111_7 + 1111_8 + 1111_9 = xyxyx_7 - 911_7 + 1111_7 + 1111_8 + 1111_9 = xyxyx_7 - 911_7 + 1111_8 + 1111_9 + 111_9 + 1111_9 + 1111_9 + 1111_9 + 1111_9 + 1111_9 + 1111_9 + 11$$

Find x + y.

(16) In what base b is the following addition correct?

$$66 + 87 + 85 + 48 = 132$$

- (17) If  $53 \times 8 = 235$  in some base b, what is b?
- (18) If 440 + 340 = 1000, what base is being used?
- (19) In what base(s) is 165 a divisor of 561?