Name: _____

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Mini-math Div 3/4: Friday, March 19, 2025 (10.10-10.15) - (25 minutes)

1. (3 points) The series $\sum_{n=1}^{\infty} \frac{(-1)^n}{n}$ converges to S. If S_n is used to approximate S, what is the least value of n for which the alternating series error bound guarantees an error to strictly within 0.01?

2. (3 points) Let P(x) be the fifth-degree Taylor Polynomial for a function f about x = 1. Information about the maximum of the absolute value of selected derivatives of f over various intervals is given below.

$$\max_{\substack{0 \le x \le 1.5 \\ 1 \le x \le 1.5 \\ |f^{(4)}(x)| = 4.6, \quad \max_{\substack{0 \le x \le 1.5 \\ 1 \le x \le 1.5 \\ |f^{(6)}(x)| = 5.1 \\ 1 \le x \le 1.5 \\ 1 \le x \le 1.5 \\ |f^{(6)}(x)| = 5.1 \\ 1 \le x \le 1.5 \\ 1 \le x \le 1$$

Find the smallest value of k for which the Lagrange error bound guarantees that

 $|f(1.5) - P(1.5)| \le k$

3. (4 points) Find the interval of convergence for the series $\sum_{n=1}^{\infty} \frac{(-1)^n (x-3)^n}{n2^n}$

4. (3 points) What is the Maclaurin series for $\frac{\cos x - 1}{x}$? Assume differentiability at 0 (e.g. the function has a value at 0 which makes it differentiable). You may, but are not required to, express your answer in summation notation.

5. (4 points) Let f be a function with f(0) = 2 and $f'(x) = \arctan x$. Write the first three non-zero terms of the Maclaurin series for f.