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Mini-math Div 3/4: Friday, September 13, 2024 (6.1-6.3) - 6 minutes

1. (1 point) Choose the limit of the Riemann Sum that is the integral:  $\int_2^4 \frac{1}{x+2} dx$ 

A. 
$$\lim_{n \to \infty} \sum_{k=1}^{n} \frac{1}{\frac{k}{n} + 2} \cdot \left(\frac{2}{n}\right)$$

C. 
$$\lim_{n \to \infty} \sum_{k=1}^{n} \frac{1}{\frac{k}{n} + 4} \cdot \left(\frac{2}{n}\right)$$

B. 
$$\lim_{n \to \infty} \sum_{k=1}^{n} \frac{1}{\frac{2k}{n} + 2} \cdot \left(\frac{2}{n}\right)$$

D. 
$$\lim_{n \to \infty} \sum_{k=1}^{n} \frac{1}{\frac{2k}{n} + 4} \cdot \left(\frac{2}{n}\right)$$

2. (1 point) Choose the integral that is the limit of the Riemann Sum:  $\lim_{n\to\infty}\sum_{k=1}^{n}\sin\left(1+\frac{8k}{n}\right)\cdot\frac{4}{n}$ 

A. 
$$\int_0^4 \sin(1+2x) \, dx$$

$$B. \int_1^5 \sin(1+x) \, dx$$

A. 
$$\int_0^4 \sin(1+2x) dx$$
 B.  $\int_1^5 \sin(1+x) dx$  C.  $\int_1^5 \sin(1+2x) dx$  D.  $\int_1^5 \sin x dx$ 

$$D. \int_1^5 \sin x \, dx$$

3. (1 point) Suppose f is a concave up function and the following are selected values of f:

x	0	1	3	4	6
f(x)	3	2	4	6	12

If we use the trapezoidal rule with 4 unequal subintervals to approximate  $\int_0^6 f(x) dx$ , then:

- A.  $\int_0^6 f(x) dx \approx 31.5$  and this is an underestimate
- B.  $\int_0^6 f(x) dx \approx 31.5$  and this is an overestimate
- C.  $\int_0^6 f(x) dx \approx 63$  and this is an underestimate
- D.  $\int_0^6 f(x) dx \approx 63$  and this is an overestimate