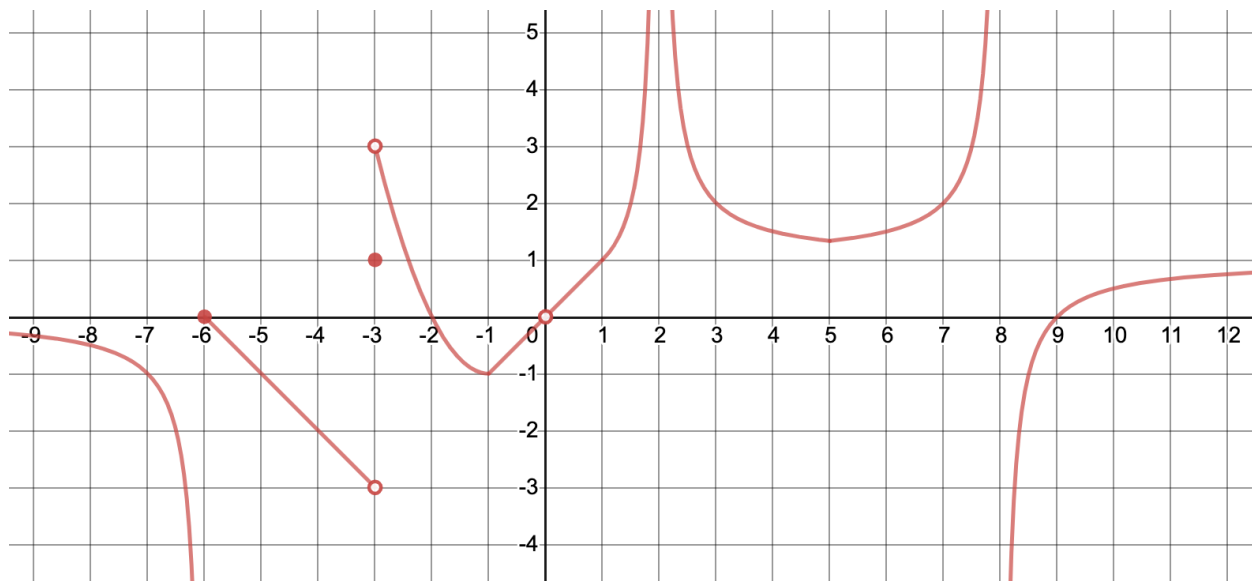


Consider the below graph of a function  $f(x)$  (integer coordinates can be assumed where clear).



Find the following limits, if they exist. If they do not, indicate whether the limit is  $\infty$ ,  $-\infty$ , or DNE. (No proofs required.)

(a)  $\lim_{x \rightarrow -\infty} f(x)$

**Solution:** 0

(f)  $\lim_{x \rightarrow -4^+} f(x)$

**Solution:** -2

(k)  $\lim_{x \rightarrow 0^-} f(x)$

**Solution:** 0

(p)  $\lim_{x \rightarrow 2} f(x)$

**Solution:**  $\infty$

(b)  $\lim_{x \rightarrow -6^-} f(x)$

**Solution:**  $-\infty$

(g)  $\lim_{x \rightarrow -4} f(x)$

**Solution:** -2

(l)  $\lim_{x \rightarrow 0^+} f(x)$

**Solution:** 0

(q)  $\lim_{x \rightarrow 8^-} f(x)$

**Solution:**  $\infty$

(c)  $\lim_{x \rightarrow -6^+} f(x)$

**Solution:** 0

(h)  $\lim_{x \rightarrow -3^-} f(x)$

**Solution:** -3

(m)  $\lim_{x \rightarrow 0} f(x)$

**Solution:** 0

(r)  $\lim_{x \rightarrow 8^+} f(x)$

**Solution:**  $-\infty$

(d)  $\lim_{x \rightarrow -6} f(x)$

**Solution:** DNE

(i)  $\lim_{x \rightarrow -3^+} f(x)$

**Solution:** 3

(n)  $\lim_{x \rightarrow 2^-} f(x)$

**Solution:**  $\infty$

(s)  $\lim_{x \rightarrow 8} f(x)$

**Solution:** DNE

(e)  $\lim_{x \rightarrow -4^-} f(x)$

**Solution:** -2

(j)  $\lim_{x \rightarrow -3} f(x)$

**Solution:** DNE

(o)  $\lim_{x \rightarrow 2^+} f(x)$

**Solution:**  $\infty$

(t)  $\lim_{x \rightarrow \infty} f(x)$

**Solution:** 1

Where is the function discontinuous? Identify the type of discontinuity at such points.

**Solution:** Removable discontinuity at 0.

Jump discontinuity at  $-3$ .

Infinite discontinuities at  $-6, 2, 8$ .