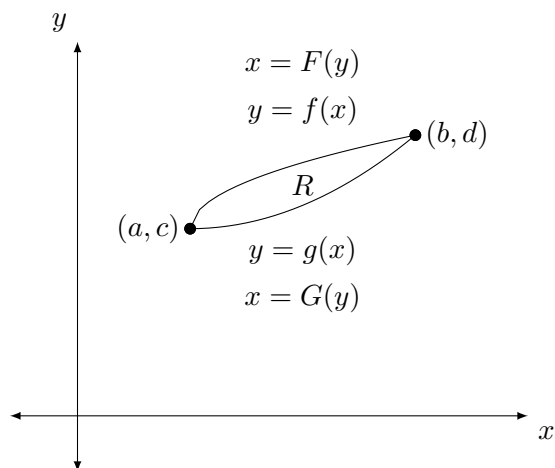


## Volumes

Suppose  $R$  is the region bounded by the curves as indicated in the below. Assume  $a < b$  and  $c < d$ .



Set up integrals for the following, but do not evaluate.

1. The volume of a solid with base given by  $R$  and whose cross-sections perpendicular to:

(a) the  $x$ -axis are squares.

(b) the  $x$ -axis are rectangles whose heights are half their width.

(c) the  $x$ -axis are right isosceles triangles whose hypotenuse is along the base.

(d) the  $x$ -axis are semi-circles.

(e) the  $y$ -axis are semi-circles.

(f) the  $y$ -axis are rectangles whose heights are three times their width.

(g) the  $y$ -axis are right isosceles triangles whose hypotenuse is not on the base.

(h) the  $y$ -axis are triangles whose heights are three times their base.

2. The volume of the solid of revolution where we revolve the region  $R$  about:

(a) the  $x$ -axis

(b) the  $y$ -axis

(c) the line  $y = -2$  (assume  $c > -2$ )

(d) the line  $x = -3$  (assume  $a > -3$ )

(e) the line  $y = 4$  (assume  $d < 4$ )

(f) the line  $x = 5$  (assume  $b < 5$ )