In 1-4, explain why the function has a zero in the given interval.

1
$$f(x) = \frac{1}{16}x^4 - x^3 + 3$$
; [1,2]

2
$$f(x) = x^3 + 3x - 2$$
; [0,1]

3
$$f(x) = x^2 - x - \cos x$$
; $[0, \pi]$

$$f(x) = -\frac{4}{x} + \tan\left(\frac{\pi x}{8}\right); [1,3]$$

In 5-8, verify that the Intermediate Value Theorem guarantees that there is a zero in the interval [0,1] for the given function. Use a graphing calculator to find the zero.

5
$$f(x) = x^3 + x - 1$$

6
$$f(x) = x^3 + 3x - 2$$

$$7 \qquad g(t) = 2\cos t - 3t$$

8
$$h(\theta) = 1 + \theta - 3\tan\theta$$

In 9-12, verify that the Intermediate Value Theorem applies to the indicated interval and find the value of *c* guaranteed by the theorem. No calculator is permitted on these problems.

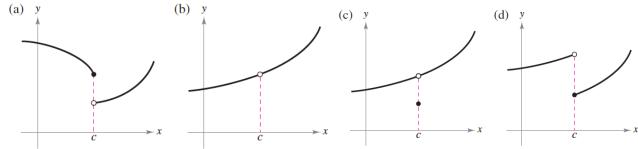
9
$$f(x)=x^2+x-1, [0,5], f(c)=11$$

10
$$f(x) = x^2 - 6x + 8$$
, [0,3], $f(c) = 0$

11
$$f(x) = x^3 - x^2 + x - 2$$
, [0,3], $f(c) = 4$

12
$$f(x) = \frac{x^2 + x}{x - 1}, \quad \left[\frac{5}{2}, 4\right], \quad f(c) = 0$$

State how continuity is destroyed at x = c for each of the graphs below:



Use the Intermediate Value Theorem to show that for all spheres with radii in the interval [1,5], there is one with a volume of 275 cubic centimeters.

Show that
$$f(x)$$
 is continuous at $x = 2$ for $f(x) = \begin{cases} 5 - x, & -1 \le x \le 2 \\ x^2 - 1, & 2 < x \le 3 \end{cases}$.

Determine whether f(x) is continuous at x = -1 for $f(x) = \begin{cases} \frac{1}{x}, & x \le -1 \\ \frac{x-1}{2}, & -1 < x < 1 \end{cases}$